

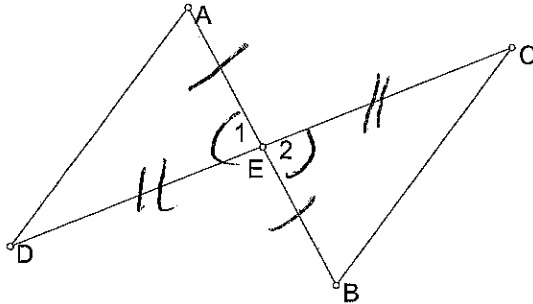
Name Key

201 Chapter 4: Proofs

#2 + #5
the D moved =
#11 notation

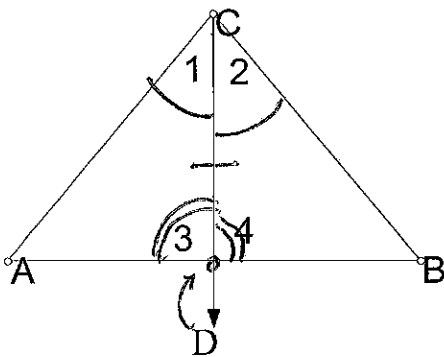
Mrs. Hayden

1. Given: E is the midpoint of \overline{AB} and \overline{CD}
Prove: $\angle D \cong \angle C$



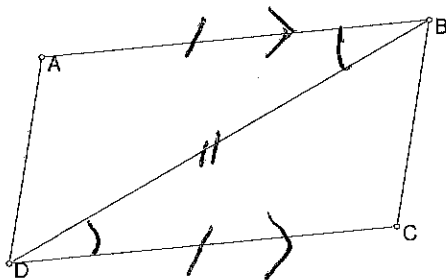
Statements	Reasons
① \sim	① Given
② $AE \cong BE$ $DE \cong CE$	② def of Midpt
③ $\angle 1 \cong \angle 2$	③ Vert Ls \cong
④ $\triangle AED \cong \triangle BEC$	④ SAS
⑤ $\angle D \cong \angle C$	⑤ CPCTC

2. Given: \overrightarrow{CD} bisects $\angle ACB$; $\angle 3 \cong \angle 4$
Prove: $\angle A \cong \angle B$



Statements	Reasons
① \sim	① Given
② $\angle 1 \cong \angle 2$	② def of \angle bis
③ $\overline{CD} \cong \overline{CD}$	③ Reflexiv
④ $\triangle ACD \cong \triangle BCD$	④ ASA
⑤ $\angle A \cong \angle B$	⑤ CPCTC

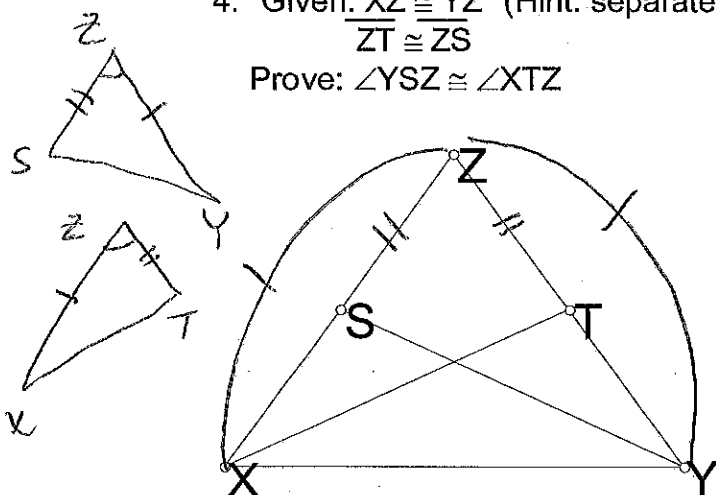
3. Given: $\overline{AB} \cong \overline{CD}$; $\overline{AB} \parallel \overline{CD}$
Prove: $\overline{AD} \cong \overline{CB}$



Statements	Reasons
① \sim	① Given
② $\overline{AB} \cong \overline{CD}$	② Reflexiv
③ $\angle ABD \cong \angle CDB$	③ Alt. Int \angle s thm
④ $\triangle ABD \cong \triangle CDB$	④ SAS
⑤ $\overline{AD} \cong \overline{CB}$	⑤ CPCTC

4. Given: $\overline{XZ} \cong \overline{YZ}$ (Hint: separate the triangles)
 $\overline{ZT} \cong \overline{ZS}$

Prove: $\angle YSZ \cong \angle XTZ$

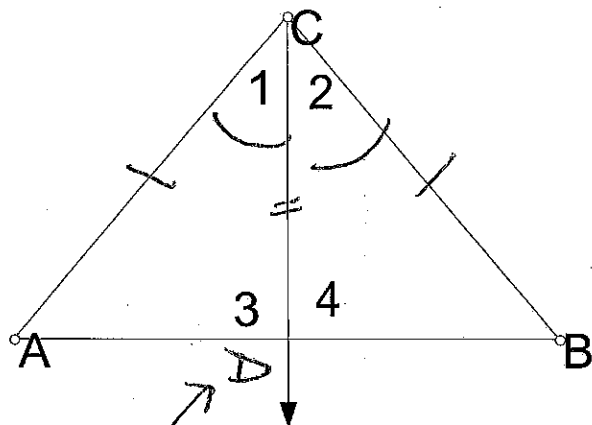


Statements

Reasons

- | | |
|---------------------------------------|-------------|
| ① ~ | ① Given |
| ② $\angle Z \cong \angle Z$ | ② Reflexive |
| ③ $\triangle XZS \cong \triangle YZT$ | ③ SAS |
| ④ $\angle XSZ \cong \angle YTZ$ | ④ CPCTC |

5. Given: $\overline{AC} \cong \overline{BC}$; $\angle 1 \cong \angle 2$
 Prove: $\overline{DA} \cong \overline{DB}$

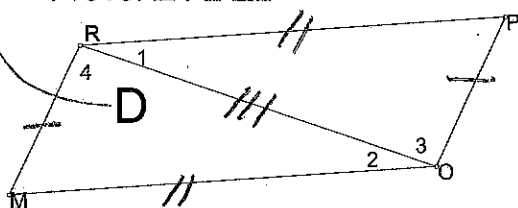


Statements

Reasons

- | | |
|---------------------------------------|-------------|
| ① ~ | ① Given |
| ② $\overline{CD} \cong \overline{CD}$ | ② Reflexive |
| ③ $\triangle ADC \cong \triangle BDC$ | ③ SAS |
| ④ $\overline{DA} \cong \overline{DB}$ | ④ CPCTC |

6. Given: $\overline{MO} \cong \overline{PR}$; $\overline{RM} \cong \overline{OP}$
 Prove: $\angle 1 \cong \angle 2$

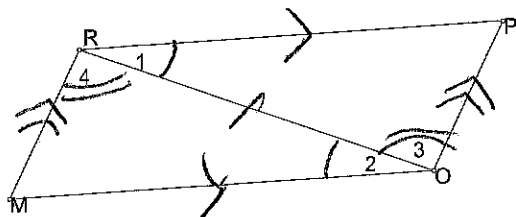


Statements

Reasons

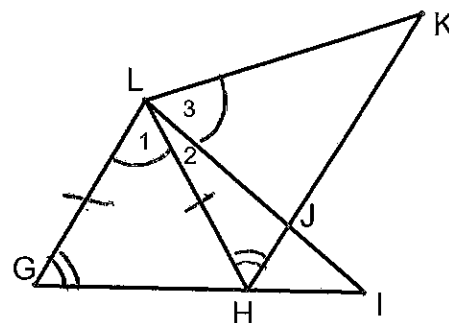
- | | |
|---------------------------------------|-------------|
| ① ~ | ① Given |
| ② $\overline{RO} \cong \overline{RO}$ | ② Reflexive |
| ③ $\triangle ROP \cong \triangle ORM$ | ③ SSS |
| ④ $\angle 1 \cong \angle 2$ | ④ CPCTC |

7. Given: $\overline{RP} \parallel \overline{OM}$; $\overline{RM} \parallel \overline{PO}$
 Prove: $\overline{RM} \cong \overline{OP}$



Statements	Reasons
① ~	① Given
② $\overline{RO} \cong \overline{RO}$	② Reflexive
③ $\angle 1 \cong \angle 2$; $\angle 3 \cong \angle 4$	③ Alt/Int \angle s Thm
④ $\triangle ROP \cong \triangle ORM$	④ ASA
⑤ $\overline{RM} \cong \overline{OP}$	⑤ CPCTC

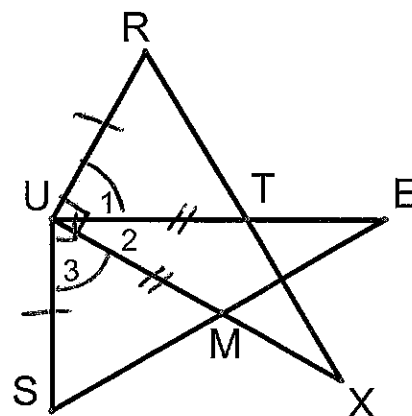
8. Given: $m\angle 1 = m\angle 3$; $\overline{LG} \cong \overline{LH}$; $\angle G \cong \angle LHJ$
 Prove: $\triangle GLI \cong \triangle HLK$



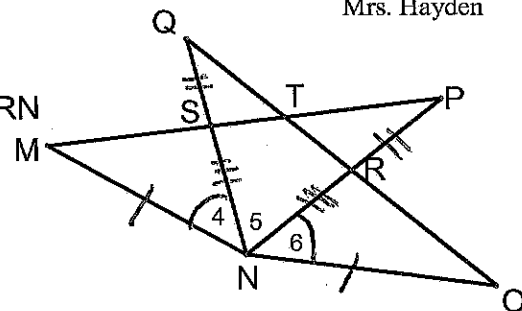
Statements	Reasons
① ~	① Given
② $m\angle 2 = m\angle 2$	② Reflexive
③ $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 2$	③ Addition
④ $m\angle 1 + m\angle 2 = m\angle GLI$ $m\angle 3 + m\angle 2 = m\angle HLK$	④ AA P.
⑤ $m\angle GLI = m\angle HLK$	⑤ Subs.
⑥ $\angle GLI \cong \angle HLK$	⑥ def of \cong
⑦ $\triangle GLI \cong \triangle HLK$	⑦ ASA

9. Given: $\overline{RU} \perp \overline{UM}$; $\overline{UT} \perp \overline{US}$; $\overline{UT} \cong \overline{UM}$; $\overline{UR} \cong \overline{US}$
 Prove: $\overline{TR} \cong \overline{MS}$

Statements	Reasons
1. ~	1. Given
2. $\angle 1$ & $\angle 2$ are compl.	2. If the non-adjacent sides of two acute \angle s are \perp , then the \angle s are complementary.
3. $\angle 3$ & $\angle 2$ are compl.	3. (same as #2)
4. $\angle 1 \cong \angle 3$	4. \cong Compl. Thm
5. $\triangle UTR \cong \triangle UMS$	5. SAS
6. $\overline{TR} \cong \overline{MS}$	6. CPCTC



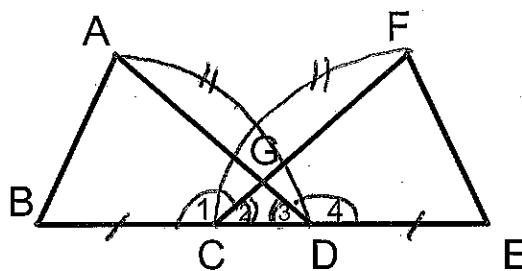
10. Given: $m\angle 4 = m\angle 6$; $\overline{MN} \cong \overline{NO}$; $QS = PR$; $SN = RN$
 Prove: $\triangle MNP \cong \triangle ONQ$



Statements	Reasons
① $\overline{MN} \cong \overline{NO}$	① Given
② $m\angle 5 = m\angle 5$	② Refl
③ $m\angle 4 + m\angle 5 = m\angle 6 + m\angle 5$	③ Add
④ $m\angle 4 + m\angle 5 = m\angle MNP$	④ AAP
⑤ $m\angle 6 + m\angle 5 = m\angle ONQ$	⑤ AAP
⑥ $m\angle MNP = m\angle ONQ$	⑥ Subst
⑦ $\angle MNP \cong \angle ONQ$	⑦ def \cong
⑧ $QS + SN = PR + RN$	⑧ Add
⑨ $QS + SN = QN$ $PR + RN = PN$	⑨ SLP
⑩ $QN = PN$	⑩ Subst
⑪ $\overline{QN} \cong \overline{PN}$	⑪ def \cong
⑫ $\triangle MNP \cong \triangle ONQ$	⑫ SAS

Notation * 11. Given: $\overline{BC} \cong \overline{DE}$; $\angle 1 \cong \angle 4$; $\overline{AD} \cong \overline{FC}$
 Prove: $\overline{AB} \cong \overline{FE}$

Statements	Reasons
① $\overline{BC} \cong \overline{DE}$	① Given
② $\angle 1 + \angle 2$ are LP $\angle 4 + \angle 3$ are LP	② def \angle LP
③ $\angle 1 + \angle 2$ are suppl. $\angle 4 + \angle 3$ are suppl.	③ LPP
④ $\angle 2 \cong \angle 3$	④ \cong suppl. thm
⑤ $CD = CD$	⑤ Refl
⑥ $BC + CD = CD + DE$	⑥ Add
⑦ $BC + CD = BD$ $CD + DE = CE$	⑦ SAP
⑧ $BD = CE$	⑧ Subst
⑨ $\overline{BD} \cong \overline{CE}$	⑨ def \cong
⑩ $\triangle ABD \cong \triangle FEC$	⑩ SAS



⑪ $\overline{AB} \cong \overline{FE}$ ⑫ CPCTC